

**Rationalizing and Trigonometric Substitutions**

Rationalizing Substitutions

Integrands involving  $\sqrt[n]{ax + b}$

EX 1  $\int \frac{x^2 + 3x}{\sqrt{x+4}} dx$

EX 2  $\int \frac{\sqrt{x}}{x+1} dx$

Integrals involving  $\sqrt{a^2 - x^2}$ ,  $\sqrt{a^2 + x^2}$ ,  $\sqrt{x^2 - a^2}$ ,  $a \in \mathfrak{R}$

a)  $\sqrt{a^2 - x^2} \rightarrow \text{let } x = a \sin \theta \quad \theta \in [-\pi/2, \pi/2]$

b)  $\sqrt{a^2 + x^2} \rightarrow \text{let } x = a \tan \theta \quad \theta \in (-\pi/2, \pi/2)$

c)  $\sqrt{x^2 - a^2} \rightarrow \text{let } x = a \sec \theta \quad \theta \in [0, \pi], \theta \neq \pi/2$

EX 3  $\int \frac{x^2}{\sqrt{16 - x^2}} dx$

EX 4  $\int_2^3 \frac{dt}{t^2 \sqrt{t^2 - 1}}$

Completing the Square (Use this strategy when there is a quadratic expression in the radical.)

$$\text{EX 5 } \int \frac{3x}{\sqrt{x^2 + 4x - 5}} dx$$