

Math5700 Notes
Section 2.1.2-2.1.3

Starters:

1. Use the Division Algorithm to write $\frac{179}{7}$ as a decimal.

2. Convert $3.012\overline{351}$ to a fraction.

Theorem 2.6: When is a proper fraction a terminating decimal? And how can we tell that it terminates in t digits after the decimal?

Theorem 2.8: What happens if the denominator of a proper fraction (in reduced form) has no 2 nor 5 as prime factors?

Theorem 2.7: Derive a formula for simple-periodic decimal, x (that's between 0 and 1), with period p .

$$\text{Let } x = 0.\overline{d_1 d_2 d_3 \dots d_p} .$$

Theorem 2.9 & 2.10: What if $x = 0.d_1d_2d_3\dots d_t \overline{d_{t+1}d_{t+2}d_{t+3}\dots d_{t+p}}$?

Examples:

- (a) Find decimal representations for $\frac{1}{27}$ and $\frac{1}{37}$.

(b) Can you find another similar example?

2. Consider reciprocals of primes that have simple-periodic decimal representations.

(a) Show there is exactly one with period $p = 1$. What is it?

(b) Show there is exactly one with period $p = 2$. What is it?

(c) Show there is exactly one with period $p = 3$. What is it?

(d) Show there are exactly two with period 5. What are they?

3. Use the formula for a geometric series to write $0.\overline{345}$ and $0.3\overline{45}$ as reduced fractions.