

**Math5700, Capstone Course, Spring 2013**  
**Homework 3**

Name: \_\_\_\_\_

Date: \_\_\_\_\_

(Please staple this as the cover sheet to the Homework #3 that you turn in.)

1. Solve these inequalities.

(a)  $|4-2x|+1 \geq 11$

(b)  $(y+4)^4+5 < 0$

(c)  $\frac{2x^2+10x-16}{x-4} \leq 3$

(d)  $\log_4(w-1)^4+2 \leq \log_4(2w-2)$

(e)  $\log_4(w-1)^3+2 \leq \log_4(2w-2)$

(f)  $-2(9^{x^6-1}) \geq 36$

(g)  $x(2x-1)(x-3)^2 < 0$

(h)  $\frac{1}{x+2} \geq \frac{2}{x-2}$

2. If you're given this inequality  $\frac{13}{31} < \frac{8}{19}$  and you need to verify if it is in fact correct, how would you explain this to your students (without a calculator)? And, would it be reasonable to "cross multiply" to check the validity of the statement? Why or why not?

What if the inequality is  $-\frac{13}{31} < -\frac{8}{19}$  instead?

What if the inequality is  $\frac{13}{31} < \frac{8}{19x}$  instead?

3. In which setting or under what conditions do you need to consider cases in solving an inequality?

4. Simplify these expressions.

(a)  $\sqrt{x^2}$

(b)  $(\sqrt{x})^2$

(c)  $\sqrt[3]{x^3}$

(d)  $\sqrt{(-3)^2}$