uid number: ______ Special number: _____

Instructions:

- Please show all of your work as partial credit will be given where appropriate, **and** there may be no credit given for problems where there is no work shown.
- All answers should be completely simplified, unless otherwise stated.
- There are no calculators or any sort of electronics allowed on this exam. Make sure all cell phones are put away and out of sight. If you have a cell phone out at any point, for any reason, you will receive a zero on this exam.
- You will be given an opportunity to ask clarifying questions about the instructions at exactly 8:40 a.m. (for a couple minutes). The questions will be answered for the entire class. After that, no further questions will be allowed, for any reason.
- You must show us your U of U student ID card when finished with the exam.
- The exam key will be posted on Canvas by noon.
- Somewhere on this exam, you may need to know

$$D_x(\arctan x) = \frac{1}{1+x^2}$$

- You may ask for scratch paper. You may use NO other scratch paper. Please transfer all finished work onto the proper page in the test for us to grade there. We will <u>not</u> grade the work on the scratch page.
- You are allowed to use one 8.5x11 inch piece of paper with notes for your reference during the exam.

(This exam totals 100 points, not including the extra credit problem.) STUDENT—PLEASE DO NOT WRITE BELOW THIS LINE. THIS TABLE IS TO BE USED FOR GRADING.

Problem	Score
1 & 2	
3	
4 & 5	
6 & 7	
8	
9	
EC	

1. (12 pts) Find the directional derivative of $f(x,y,z)=x^2y^2+yz^3-4xyz$ at p=(3,0,1) in the direction of a=i-2j+2k.

from P(-4, 0.25) to Q(-4.01, 0.26) for $z = \arctan(xy)$.

Answer: _____

3. (10 pts) Find the two points on the 3-d surface $F(x,y,z)=x^2+2y^2-z^2-7=0$ where the tangent plane is parallel to the plane 3x+2y-2z=15.

Answer : ______

4. (10 pts) Give the domain for where this function (that lives in 4-d space) is continuous.

$$f(x, y, z) = \frac{3xy}{\ln(25 - x^2 - y^2 - z^2)}$$

Answer:	

5. (15 pts) For $e^{xy} + x \sin y + 2z^2 = 9$, find the equation of the tangent plane at the input **point (2, 0), in the first octant**. (Hint: In other words, when you get the full point on the surface for this plane, you may have two z-coordinates and thus two points to choose from. Choose the point in the first octant of 3-d space, where all x, y, and z-values are positive.)

6. (10 pts) Given $w(x,y)=2x^3-xy+2y^2$, $x^3=u-v$, y=uv, answer these questions.

(a) Write out the chain rule for $\frac{\partial w}{\partial u}$ that you need to use for this problem.

(b) Find $\frac{\partial w}{\partial u}$ when u=-3, v=-2.

Answer :_____

8. (a) (5 pts) Convert $4x^2+4y^2=25y$ from a Cartesian coordinate equation into an equation in cylindrical coordinates.

Answer : _____ (b) (5 pts) Convert $(2\sqrt{2},-2\sqrt{2},4\sqrt{3})$ from Cartesian coordinates into spherical coordinates.

9. (13 pts) Find all critical and saddle points for $f(x, y) = x^3 + y^2 - 3x^2 + 2y + 4$. Determine whether each point is a minimum, maximum or saddle point. Critical point(s) (Specify whether they're min, max or saddle.): Note: Give FULL 3-d points.

Extra Credit: (5 pts) Answer each of these short answer questions.

- 1. Circle all of the following statements that are true. (It's possible more than one of these statements is correct.)
 - (a) The vector $\langle f_x(x,y) \rangle$, $f_y(x,y)$, $-1 \rangle$ is perpendicular to the surface z = f(x,y) at the point (x,y).
 - (b) The vector $\langle f_x(x,y), f_y(x,y) \rangle$ is perpendicular to the surface z = f(x,y) at the point (x,y).
 - (c) The vector $\langle f_x(x,y), f_y(x,y) \rangle$ is perpendicular to the level curve of the surface z = f(x,y) at the point (x,y).
- 2. Which of the following two statements is true? (circle one)
 - (a) If f is continuous at (x, y), then it's differentiable there.
 - (b) If f is differentiable at (x, y), then it's continuous there.
- 3. If $\lim_{y\to 0}f(y\,,y)=L$, then $\lim_{(x,\,y)\to(0,0)}f(x\,,y)=L$. True or False (circle one)
- 4. The level curves for $z = \sqrt{25 2x^2 y^2}$ are circles.

True or False (circle one)

If your answer is false, then state what shape the level curves are:
