



5. (10 pts) Choose a topic: a) Rigor in Calculus or b) Apollonius' conic sections and write a short summary.

6. (10 pts) Give either a) a short history of the solution of the cubic equation, or b) a short history of the reform of astronomy begun in the 16th century.

7. (12 pts) Write the discoverer/inventor for the following symbols.

+	
=	
dx	
f'	
letters as variables	
decimal fractions with decimal point	

8. (10 pts) Find the first four terms of the power series expansion of  $(1+x)^{2/3}$  using Newton's method.

9. (8 pts) Find  $d(x^x)$  using Leibniz' techniques (hint: first take a logarithm and use the fact that  $d(\log z) = dz/z$ ).

10. (8 pts) Use Fermat's technique of "adequality" (either one) to find the locations of the potential maximum and minimum values of the function  $x^3 - ax$ .

11. (8 pts) Find the length of the subnormal  $v$  to the curve  $y = x^{3/2}$  at  $x = 2$ .

12. (8 pts) Give a short account of a) the brachistochrone problem and its solution or b) Diophantus' work and notation.

13. (6 pts) Give short definitions/explanations of the following astronomical concepts:

a. celestial equator

b. ecliptic

c. declension

**Bonus problem:** Give an example of an infinitely differentiable function with no Taylor series (or more precisely, a Taylor series that converges only at a single point) and explain it.