

Math 3070 § 1.  
Treibergs

**Black Forest Example:  
One-Sample CI for  $\sigma$ .**

Name: Example  
June 2, 2011

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**Data File Used in this Analysis:**

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```
# Math 3070 - 1   Age of Black Forest Mineral           June 2, 2011
# Treibergs
#
# Data taken from Larsen & Marx, "An Introduction to Mathematical Statistics
# and its Applications, 4th. ed.," Pearson/Prentice Hall 2006. In D. McIntyre's
# 1963 study of dating rocks, the age of several samples of a particular mineral
# of known age found in the Black Forest were measured using Potassium-Argon
# dating.
# The question is how much variability is inherent in the dating method?
# The dates are in millions of years.
EstAge
249
254
243
268
253
269
287
241
273
306
303
280
260
256
278
344
304
283
310
```

---

**R Session:**

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R version 2.10.1 (2009-12-14)  
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ISBN 3-900051-07-0

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[R.app GUI 1.31 (5538) powerpc-apple-darwin8.11.1]

[Workspace restored from /Users/andrejstreibergs/.RData]

```
> tt <- read.table("M3074BlackForestdata.txt",header=T)
> tt
```

```
  EstAge
1     249
2     254
3     243
4     268
5     253
6     269
7     287
8     241
9     273
10    306
11    303
12    280
13    260
14    256
15    278
16    344
17    304
18    283
19    310
```

```
> s2 <- var(EstAge); s2
[1] 733.4327
```

```
> n <- length(EstAge); n
[1] 19
```

```
> # Two sided CI for  $\sigma^2$ .  $(n-1)S^2/\sigma^2$  has chi sq dist with  $df=n-1$ 
> # Do it at  $\alpha=.05$  level.
```

```
>
> alpha <- .05
> chi2a2 <- qchisq(alpha/2,df=n-1); chi2a2
[1] 8.308339
> chi21ma2 <- qchisq(alpha/2,df=n-1,lower.tail=F); chi21ma2
[1] 31.33573
```

```
>
> # two sided CI for  $\sigma^2$ 
> c( (n-1)*s2/chi21ma2, (n-1)*s2/chi2a2)
[1] 421.3015 1588.9806
```

```
>
> # two sided CI for  $\sigma$ 
```

```
> c( sqrt((n-1)*s2/chi21ma2), sqrt((n-1)*s2/chi2a2))
[1] 20.52563 39.86202
> # an estimate on the precision of the method.
>
> # Check to see if data is reasonably normal.
> # Needed for dist of S^2 to be chisq with df = n-1
> y <- (EstAge-mean(EstAge))/sd(EstAge)
> qqnorm(y,main="Normal QQ plot of Estimated Age",ylab="Standardized Estimated Age")
> abline(0,1,col=2)
>
> # Normal QQ plot is reasonably linear so no strong evidence of non-normal.
```

Normal QQ plot of Estimated Age

